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## **INDUSTRIAL GAS TURBINE ENGINE OFF-DESIGN PERFORMANCE IMPROVEMENT CONTROLLING COOLING AIR FLOW**

The modern gas turbine engine has been used in current power generation industry for almost half a century. They are designed to operate with the best efficiency during normal operating conditions and at specific operating points. However, due to power grid demands, different ambient temperatures, fuel types, relative humidity and driven equipment speed the gas turbine units have to work today on partial load too, which can affect the hot gas path condition and life expectancy. At these off-design conditions, gas turbine's efficiency and life deterioration rate might significantly deviate from the design specifications. In this paper, a digital twin concept for gas turbine unit off-design performance prediction (AxSTREAM® platform) is used. The description of created digital twin is presented. The validation of proposed gas turbine unit digital twin is carried out by comparison with literature source test data. The GTU performance estimation controlling cooling air at part load modes using digital twin was performed.

**Key words:** gas turbine unit digital twin, gas turbine unit, off-design mode, power control, cooling system control, efficiency improvement.

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## **УВЕЛИЧЕНИЕ ПРОИЗВОДИТЕЛЬНОСТИ ПРОМЫШЛЕННОГО ГАЗОТУРБИННОГО ДВИГАТЕЛЯ ПУТЕМ РЕГУЛИРОВАНИЯ РАСХОДА ОХЛАЖДАЮЩЕГО ВОЗДУХА**

Современный газотурбинный двигатель используется в энергетике уже почти полвека. Они предназначены для работы с максимальной эффективностью при нормальных рабочих условиях и в конкретных рабочих точках совместной работы турбины и компрессора. Тем не менее, из-за требований электросети, изменения температуры окружающей среды, типа топлива, относительной влажности или частоты вращения приводного устройства, газотурбинные установки вынуждены сегодня работать при частичной нагрузке, что может повлиять на состояние проточной части турбины и продолжительность ее жизни. При этих внепроектных условиях эффективность газовой турбины и коэффициент износа могут значительно отличаться от проектных спецификаций. В данной статье используется концепция цифрового двойника объекта для прогнозирования производительности турбоагрегата на внепроектных режимах (платформа AxSTREAM®). Представлено описание созданного цифрового двойника. Валидация предлагаемого цифрового двойника газотурбинной установки осуществляется путем сравнения с данными испытаний приведенными в источниках литературы. Была выполнена оценка производительности ГТУ, при управлении расходом охлаждающего воздуха на режимах частичной нагрузки с использованием цифрового двойника.

**Ключевые слова:** цифровой двойник газотурбинного агрегата, газотурбинный агрегат, режим внепроектной работы, управление мощностью, управление системой охлаждения, повышение эффективности.

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## **ЗБІЛЬШЕННЯ ПРОДУКТИВНОСТІ ПРОМИСЛОВОГО ГАЗОТУРБИННОГО ДВИГУНА ШЛЯХОМ РЕГУЛЮВАННЯ ВИТРАТИ ОХОЛОДЖУЮЧОГО ПОВІТРЯ**

Сучасний газотурбинний двигун використовується в енергетиці вже майже півстоліття. Вони призначені для роботи з максимальною ефективністю при нормальних робочих умовах і в конкретних робочих точках спільної роботи турбіни і компресора. Проте, через вимоги електромережі, зміни температури навколишнього середовища, типу палива, відносної вологості або частоти обертання приводного пристрою, газотурбинні установки змушені сьогодні працювати при частковому навантаженні, що може вплинути на стан проточної частини турбіни і тривалість її життя. При цих внепроектних умовах ефективність газової турбіни і коефіцієнт зносу можуть значно відрізнятися від проектних специфікацій. У даній статті використовується концепція цифрового двійника об'єкта для прогнозування продуктивності турбоагрегату на позапроектних режимах (платформа AxSTREAM®). Представлено опис створеного цифрового двійника. Валидація запропонованого цифрового двійника газотурбинної установки здійснюється шляхом порівняння з даними випробувань наведеними в джерелах інформації. Була виконана оцінка продуктивності ГТУ, при регулюванні витрати охолоджуючого повітря на режимах часткового навантаження з використанням цифрового двійника.

**Ключові слова:** цифровий двійник газотурбинного агрегату, газотурбинний агрегат, режим внепроектної роботи, управління потужністю, управління системою охолодження, підвищення ефективності.

### **Introduction**

Gas turbines are widely used all over the world. The same GTU frame could be installed in arctic or desert regions providing significantly different environmental conditions. But even little change of boundary conditions causes a significant influence on integral characteristics and reliability of the engine. It is well known, that ambient temperature elevation leads to unit efficiency and power deterioration and vice versa when the turbine inlet temperature is fixed [1, 2].

There are two main reasons for GTU off-design operation:

- Environment-induced off-design.
- Grid demands or driven device induced off-design.

Environment-induced off-design is not desired in terms of driven equipment. It is usually a subject to mitigation utilizing the approaches that help to save fixed GTU power with ambient temperature rise [3]:

- Chiller application at compressor inlet.
- Water evaporation at compressor inlet.
- Humid air/steam injection to combustor

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chamber.

The off-design induced by grid demands or driven device can be achieved in several ways [4]. In the current paper, the part-load modes were carried out by turbine inlet temperature reduction. The reduction of temperature is carried out by the decline of injected fuel MFR in the combustor. The compressor inlet MFR, in this case, is almost unaltered and equal to the MFR at design mode.

One of the crucial aspects in off-design performance estimation is a determination of joint operation point of turbine and compressor to check if GTU would reliably operate avoiding any excessive temperatures of turbine blades and surge zones of the compressor and produce a certain amount of power.

The overall approach to search joint operation point is a utilization of the turbine and compressor maps (graphical method) [5, 6]. Maps utilization method is pretty simple and in combination with thermodynamic simulation allow calculating of GTU performance in the shortest time. However, the cooling system presence contributes the necessity of determining of additional factors (parameters), which leads to some simplifications and, as a consequence, may lead to inaccuracies, when maps are used. Some of these simplifications are a determination of cooling air mass flow rate (MFR) as a percent from compressor inlet air MFR and simplified GTU components geometry consideration.

There are many papers devoted to an accurate off-design performance calculation without maps utilization [7, 8]. However, their utilization is time-consuming.

Therefore the methods that allow accounting for advantages of iteration maps method (relatively short time of calculation) with the 1D calculation of compressor, turbine and cooling system are of interest. The automation of off-design GTU parameters search process makes possible excluding errors related to transferring of large amounts of data for multiple variables.

Simulation of cooled GTU requires a utilization of various 0D, 1D, 2D and 3D models for calculation of GTU components (compressor, turbine, combustor, cooling system etc.), the presence of efficient data transfer between the models and ability to incorporate custom models, and use logical operations and perform optimizations. The complex of the mentioned tools, methods, models, scripts connected in a logical sequence is essentially a digital twin of gas turbine unit (GTU DT). The development and validation of such a GTU DT are presented in this paper.

The digital twin capabilities are especially interesting for optimization tasks. By the authors, the performance augmentation of GTU using developed digital twin by cooling air MFR control is performed.

## Nomenclature

### Symbols:

GTU – gas turbine unit;  
GTU DT – gas turbine unit digital twin;  
MFR – mass flow rate;  
AEF – air excess factor;  
LHV – lower heating value;  
G – mass flow rate;  
P – pressure;  
T – temperature;  
eff – efficiency;  
N – power.

### Indexes:

extr – extraction;  
in – inlet parameters;  
out – outlet parameters;  
turb – turbine;  
comp – compressor;  
comb – combustor.

## GTU prototype for GTU DT

The 166 MW single shaft power generation stationary GTU was selected as a prototype, the digital twin will be developed for.

In the scope of this study, it was decided to limit the number of components and systems to be included in digital twin: compressor, combustor, turbine and cooling system (**Figure 1**). The thermo-structural analysis was not considered in this paper. However, it is planned to include it and expand the number of considered systems in future studies.

The main parameters of GTU prototype are presented in **Table 1**. Shaft rotational speed is constant for every off-design mode and equals the design mode.

The compressor is 17 stage machine with IGV and three extractions to cooling system: after nozzle of the 11<sup>th</sup> stage, after rotor of 16<sup>th</sup> stage and at compressor outlet.

Turbine is a three-stage axial machine with 14 cooling inductions and cooled duct at the turbine inlet.

Cooling system (**Figure 2**) is presented by three extractions in compressor part, which then divided on 14 cooling flows inducted to blades leading edges, trailing edges, tip, hub and shroud of turbine flow path.

The combustor is calculated by thermodynamic equations. Based on energy balance equations (1)–(4) the fuel MFR was received. Methane was used as a fuel.

$$I_{in\_turb} = f(P_{turb\_in}, T_{turb\_in}, AEF), \quad (1)$$

where  $I_{in\_turb}$  – turbine inlet enthalpy;

$P_{turb\_in}$  – turbine inlet pressure;

$T_{turb\_in}$  – turbine inlet temperature;

$AEF$  – air excess factor.

Table 1 – GTU design characteristics

Parameters	Units	Values
<b>Compressor</b>		
T <sub>in</sub>	K	288.15
P <sub>in</sub>	kPa	101.32
G <sub>in</sub>	kg/s	401.84
P <sub>out</sub>	kPa	1315.0
T <sub>out</sub>	K	625.85
G <sub>extr</sub>	kg/s	26.31
eff	–	0.9146
N	MW	137.17
<b>Combustor</b>		
G <sub>in</sub>	kg/s	375.53
G <sub>fuel</sub>	kg/s	9.009
AEF	–	2.41
<b>Turbine</b>		
P <sub>in</sub>	kPa	1249.25
T <sub>in</sub>	K	1550
G <sub>out</sub>	kg/s	384.51
T <sub>out</sub>	K	901.62
eff	–	0.9459
N	MW	303.67

$$G_{fuel} = \frac{G_{comb\_out} I_{turb\_in} - G_{comp\_out} I_{comp\_out}}{LHV}, \quad (2)$$

where  $G_{fuel}$  – fuel MFR;

$G_{comb\_out}$  – combustor outlet MFR;

$G_{comp\_out}$  – compressor outlet MFR;

$I_{comp\_out}$  – compressor outlet enthalpy;

$LHV$  – lower heating value.

$$G_{comb\_out} = G_{comp\_out} + G_{fuel}, \quad (3)$$

$$AEF = \frac{G_{comb\_out}}{G_{fuel} I_0}, \quad (4)$$

where  $I_0$  – stoichiometric air-fuel ratio.

AEF in the (1) is used for determination of combustor products composition that has a significant influence on enthalpy value determined for specified pressure and temperature.

The combustor outlet MFR in the first iteration was set as

$$G_{comb\_out} = G_{comp\_out}, \quad (5)$$

The initial guess for air excess factor was arbitrarily selected. The pressure drop at combustor was equal 0.05 for all calculations.

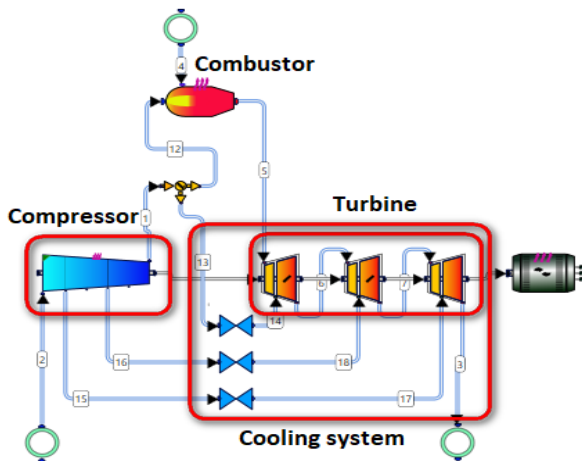


Fig. 1 – Gas turbine unit scheme

### Loss models for off-design performance prediction

Craig and Cox loss model was utilized for prediction of profile losses of the turbine nozzles and blades at the design and off-design modes. The model is empirical and based on experimental data obtained on numerous blade profiles. The authors of the loss model stated that no systematic or major discrepancies have been found in an analysis of over fifty turbines and that the most calculated values of overall efficiency being substantially within  $\pm 1.25$  percent of the measured values [10]. Besides, Ning Wei performed a study of different empirical loss models and determined that Craig and Cox loss model is one of the most accurate empirical loss models for relatively large axial turbines [11].

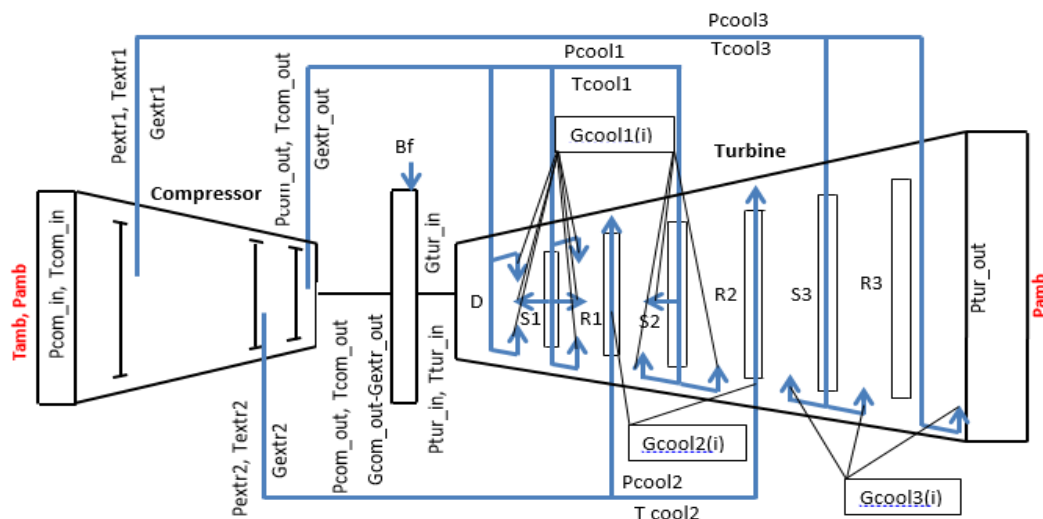


Fig. 2 – Cooling system scheme

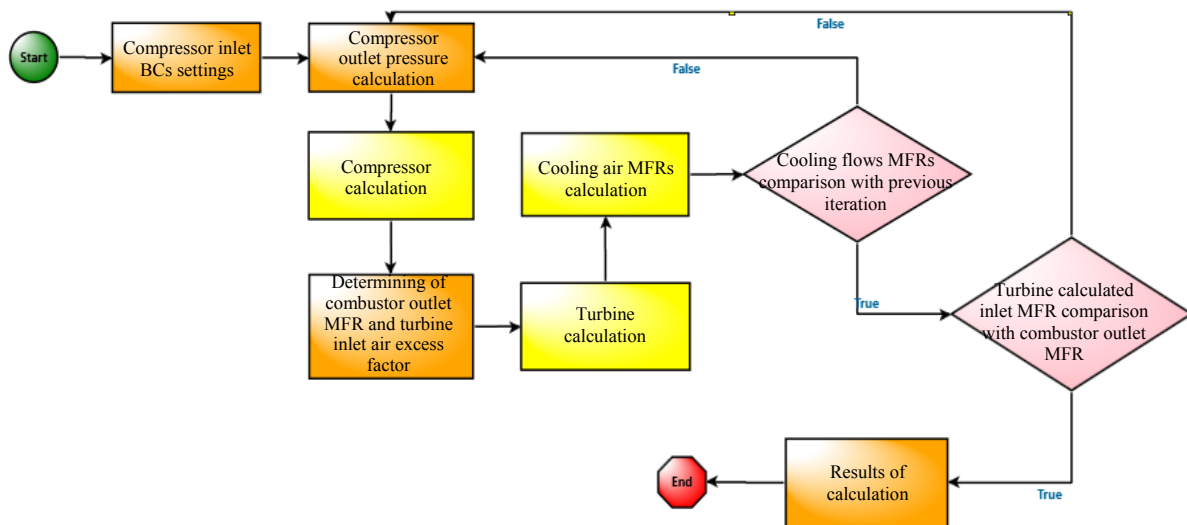


Fig. 3 – Gas turbine digital twin operation flowchart

The profile losses prediction of compressor blades were determined using the Lieblein's test data [12] approximated by Aungier [13]. In [13] author performed the validation of approximated expressions with NACA 10-stage compressor. The validation showed a good approximation of experimental data for each speed line.

The utilization of well-validated loss models for turbine and compressor served as a good foundation for the getting a high accuracy off-design performance prediction of the entire GTU. Besides, the authors performed some validation of the entire algorithm by themselves. The results are presented below in the paper.

### The description of the GTU DT

In this study digital twin is used to simulate the off-design operation of the considered GTU prototype. Turbine inlet temperature was kept constant for each off-design mode.

The scheme of calculation process is presented in **Figure 3**.

Green circle block is self-explanatory. Orange rectangles represent custom scripts. The scripts were added in order to perform additional calculations not available among off-the-shelf tools. Yellow blocks represent some available computational tool. In particular, for the compressor, it was streamline solver, as well as for turbine. For cooling system, it was hydraulic network 1D numerical solver. Pink diamonds represent conditional statements for process control according to a predefined condition. These blocks allow implementation of loops required to converge required parameter, for example, MFR for each cooling flow. The conditional block could be also used for implementation of alternative paths of the calculation process. Red octahedron is self-explanatory.

The top diamond on the diagram represents the condition of equality of cooling flows MFRs. If balances of the cooling flows mass flow rates extracted from the compressor and inducted to turbine do not correspond, the reassignment of cooling flows MFRs is performed. The equality of turbine inlet MFR and combustor outlet MFR is done by bottom diamond. In this case, the difference in mentioned above MFRs leads to reassigning of turbine inlet pressure.

All described above calculations were performed automatically. Thus, eventually, the capability to simulate off-design performance for any compressor inlet BCs as in real test facility was achieved.

### Validation of GTU DT

The validation of the developed GTU DT was performed comparing the estimated performance data with real GTU test data [10]. The comparison was performed for the off-design caused by variation of ambient temperature from +5 °C to +30 °C. The ambient pressure and turbine inlet temperature for each off-design mode were kept constant and equal to the ones at design conditions.

The pressure losses in inlet and exhaust ducts were not taken into account.

The data for power correction factor obtained utilizing the GTU DT and the GTU test data from [10] are presented in **Figure 4**. Power correction factor is a ratio of power at design mode to power at off-design mode. It is clearly seen that the power correction factor obtained on GTU DT is in good agreement with the power correction factor variation from [10]. This allows concluding that GTU DT performance data results are plausible and that GTU DT can be used for GTU off-design performance data gathering.

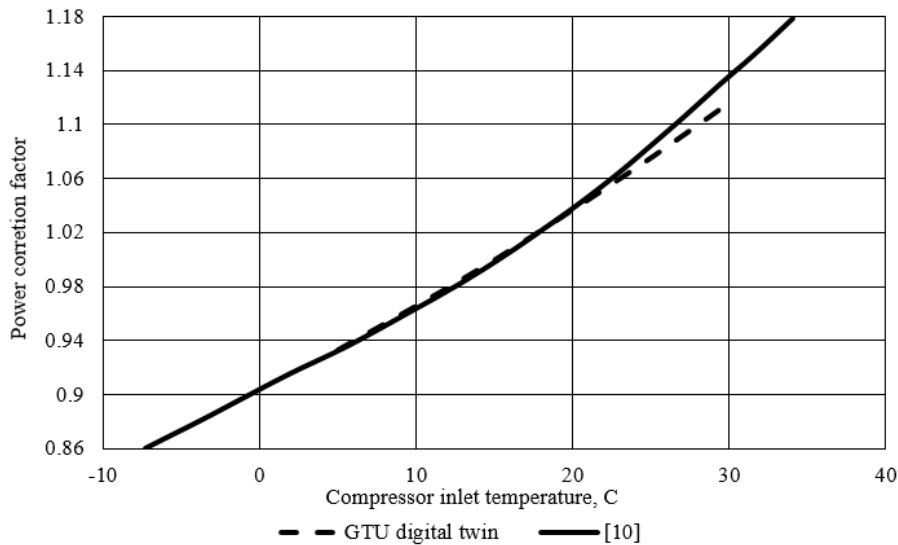


Fig. 4 – Power correction factor vs ambient temperature

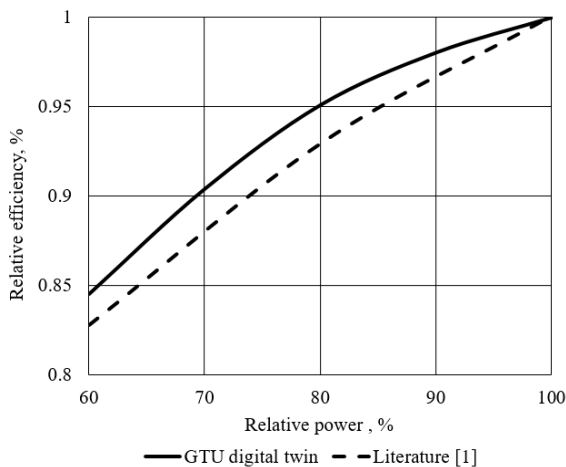


Fig. 5 – Turbine exhaust temperature vs power in relative values

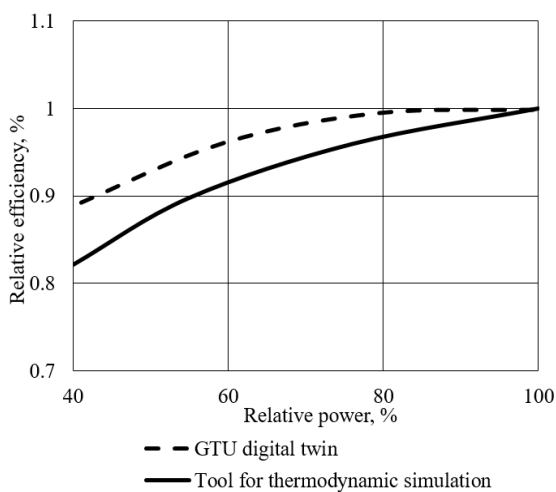


Fig. 6 – The dependency of unit efficiency from power level

Also, the validation of proposed digital twin was performed by comparison the turbine outlet temperature for different power level with generalized test data from [1] (Figure 5). The part loads of GTU are carried out by compressor inlet MFR decreasing.

The comparison of the curves showed that the obtained results are in good agreement with the trend obtained experimentally in [1], demonstrating the correctness of the results obtained on GTU virtual test facility.

#### Comparison of GTU DT results with heat balance calculation tool results

The estimation of GTU part load performance was performed utilizing the proposed VTF and utilizing cycle calculation tool with the embedded map for the compressor. The compressor map was preliminarily generated using described above streamline solver. The turbine efficiency was found based on Stodola law.

The comparison of the results is presented in this section. The dependencies of GTU efficiency determined by two mentioned approaches are presented in Figure 8.

Figure 6 shows the GTU DT results in 6 % (in relative values) difference in efficiency value at 40 % of unit power in comparison with results obtained with the conventional thermodynamic solver.

The difference can be explained by that the map was generated for fixed values of cooling flows extractions/inductions taken from design mode, but actually, the cooling flows parameters were varying for different part load modes. Its own portion of contribution into discrepancy value brought the air mass flow rate calculation method in case of map approach. Namely, it was calculated based on the simple pressure drop without taking into account variation of other thermodynamic and kinematic parameters of cool-

ing flows at extraction/induction slots of compressor/turbine flow paths. The other factor is that the cooling flows are injected into turbine stage in two sections only (upstream and downstream turbine rotor) in map approach. Besides mentioned above, the modeling of the turbine by Stodola law brought some degree of discrepancy into the results in comparison with detailed turbine simulation in streamline solver.

All mentioned above factors allows concluding that the proposed VTF results demonstrate a higher degree of accuracy in comparison with the utilized map-based approach. It should be noted that map-based approaches can be based on real field data and take into account variation of cooling flows and real compressor/turbine performance and induction/extraction slots parameters. In this case, the fidelity of the results can be rather high too. However, the advantage of VTF is that field data is not required.

### GTU performance augmentation by cooling air MFR control

It is well known that GTU part-load control by turbine inlet temperature envisages a reduction of the turbine inlet temperature to obtain the part-load mode of GTU. Authors of this paper performed simulation of part-load mode of GTU (these results are not presented here, but they will be published in ASME Turbo Expo 2018 paper) and determined that the temperature of hot gas can become even less than blades material allowable temperature, but cooling mass flow rate was almost the same as in the design mode. In other words, the cooling flow is simply wasted at deep part load modes. It is obvious to assess the possibility of cooling mass flow rate control in order to adjust it according to the temperature of hot gas and improve the efficiency of GTU at deep off-design modes.

The proposed GTU (GTU) was utilized to perform the assessment. For this, GTU cooling system was modified by the addition of control valve to the cooling channel going to first nozzle vane. The first vane required the most significant amount of cooling. Thus the effect from the reduction of cooling flow to the first nozzle has to be pretty significant.

### Determining the quantity of cooling air MFR

There are dependencies in the literary sources that allow approximately calculate the required cooling air MFR for given type of cooling and temperature of the main flow.

In the presented paper the cooling air MFR was determined from [11] (Figure 7).

$$\bar{G} = G_{cool} / G_{gas} \quad (6)$$

where  $\bar{G}$  – relative cooling air MFR;

$G_{cool}$  – cooling air MFR;

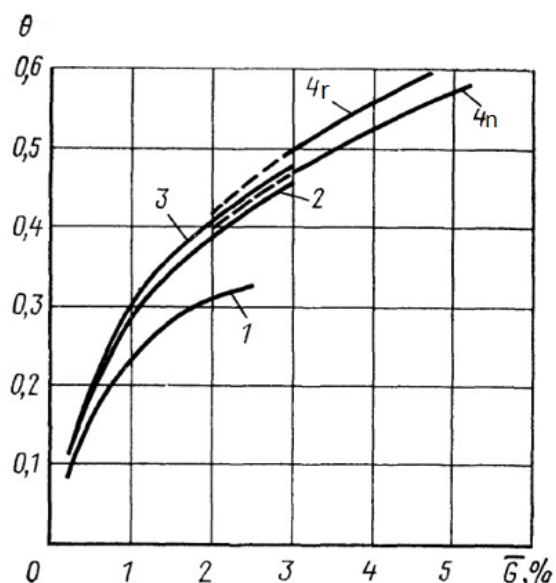


Fig. 7 – Efficiency of different types of air cooling: 1 – blade with radial channels; 2 – blade with the semi-closed cooling system; 3 – deflector blade; 4n – nozzle blade film cooling; 4r – rotor blade film cooling

$G_{gas}$  – MFR of the main flow.

$$\theta = \frac{T_{gas}^* - T_{bl}}{T_{gas}^* - T_{cool}^*} \quad (7)$$

where  $T_{gas}^*$  – total temperature of main flow;

$T_{bl}$  – maximal allowable temperature of blade without cooling;

$T_{cool}^*$  – total temperature of cooling flow.

Since the blade cooling type for presented GTU is film, the necessary cooling MFR was determined by the "4n" line.

### Results of cooling air MFR adjustment

The effect of cooling air MFR control on VGTU performance for different power levels is presented in comparison with performance without any cooling system control.

The dependency of GTU (GTU) performance for different power level is presented in Figure 8.

As we can see from Figure 8 the efficiency of GTU (GTU) with the controlled cooling system is higher than one of GTU (GTU) with the uncontrolled cooling system. The efficiency increment at 40 % of power is about 3.5% in relative values, at the 70 %, it is about 1 %. It should be noticed that cooling air MFR was controlled for first nozzle only. It can be assumed that the cooling air MFR controlling at another flow path elements allows getting even higher efficiency increments. The GTU (GTU) efficiency curve bend between 60 % and 50 % part load modes was caused by the full closure of the first nozzle cooling channel. The rest of

flow path elements have no control in this study, but GTU DT allows controlling the other cooling system branches either.

The distribution of cooling air MFR at different GTU DT power levels is presented in **Figure 9**.

It is clearly seen from **Figure 9** that the decrement of the cooling air MFR is much more significant for the case of the controlled cooling system. The turbine inlet temperature is less than the maximal allowable temperature of flow path metal in the range of 50 %–60 % of power.

It should be noticed that presented methodology of cooling system calculation allows defining the flow

directions inside the blade, which is possible at some deep part-load modes.

This assessment was not performed in this study. It is planned to include such an analysis and to perform cooling system control simulation at GTU DT part-load modes taking into account possible penetration of hot gas inside the blade and its influence on blade temperature and adjust cooling flow rate accordingly.

The dependency of relative turbine inlet temperature from power level is presented on **Figure 10**.

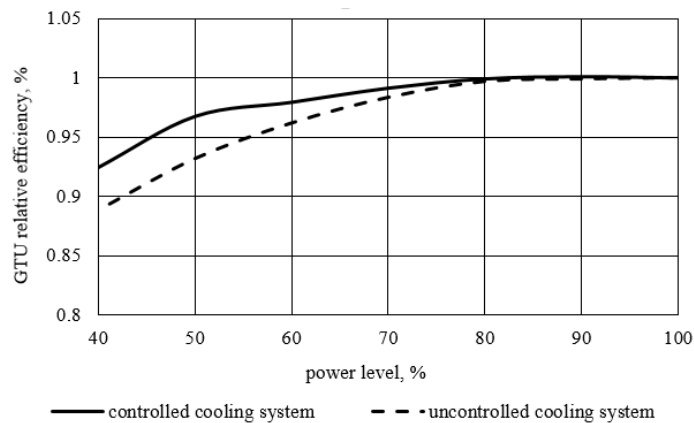


Fig. 8 – Relative GTU efficiency vs GTU power level

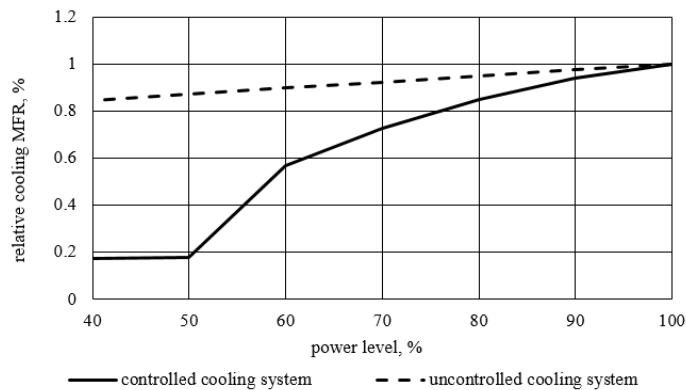


Fig. 9 – Relative cooling MFR vs GTU power level

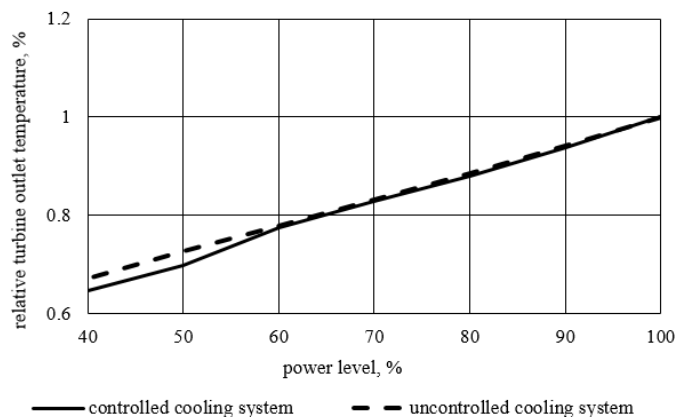


Fig. 10 – Relative turbine outlet temperature vs GTU power level

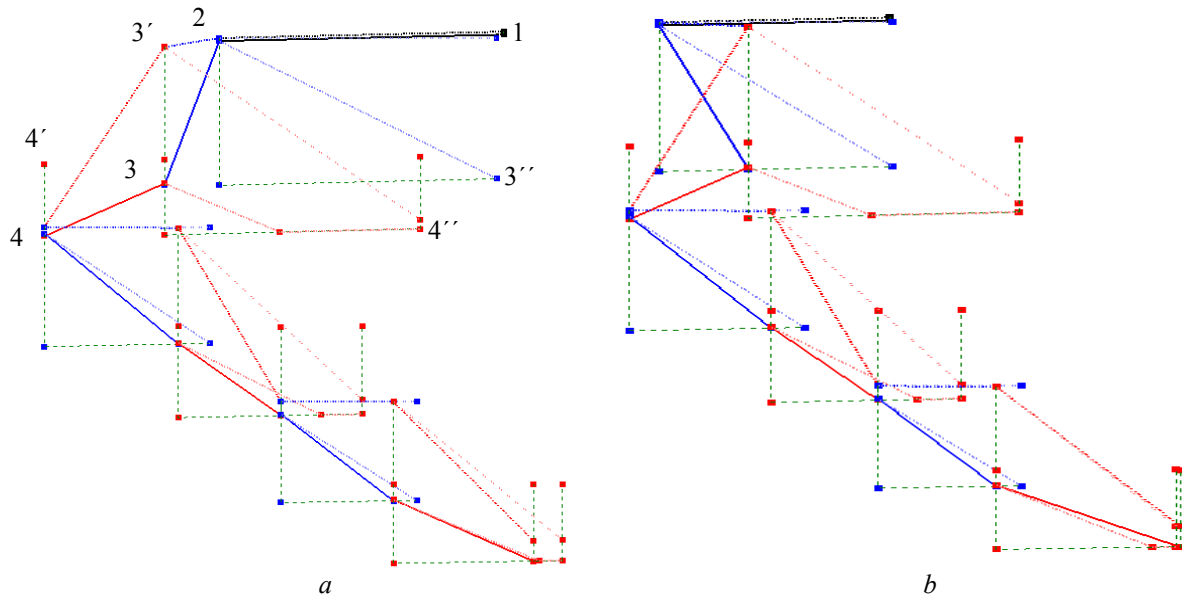


Fig. 11 – Expansion process of turbine in h-s diagram:  
 a – uncontrolled extraction; b – controlled extraction;  
 blue lines are the nozzle expansion process; red lines are the blade expansion process;  
 green verticals are isentropic expansion process; green inclined lines are isobars;  
 dark lines are expansion process in duct.

As we can see the difference in turbine outlet temperature in the range 100–60 % is not significant for controlled and uncontrolled cooling system types. The difference in 3 % in relative values is observed when the main flow temperature is less than maximal allowable metal temperature and the cooling air MFR for stationary elements is equal to zero.

The proposed digital twin allows analyzing the internal aero-thermodynamic parameters at any row of compressor and turbine flow paths and cooling channels. This is an advantage of direct performance estimation comparing to map approach. As an example, **Figure 11** represents the working fluid expansion process in the turbine taking into account cooling flows injections for both cases: controlled and uncontrolled cooling systems.

The explanation of the points and lines for the first stage of the turbine (**Figure 11**) is given below.

The 1–2 line represents the expansion process in the duct before turbine first stage.

Point 3 is the condition of gas after expansion in the first nozzle vane accounting cooling flows determined by static pressure, 3'' – the same condition without cooling accounting. Point 3' shows the total parameters of working gas after expansion in the first nozzle.

Point 4 is the total parameters in the absolute frame after first blade row accounting the cooling flows, 4'' – the same condition without cooling accounting. And the point 4' show the parameters after first blade row in the relative frame.

The dotted lines show the process without cooling. The solid lines represent a real expansion process. Blue lines represent expansion processes in stationary

nozzles. Red lines represent expansion processes in rotating blades.

### Approximate economics evaluation

Preliminary economics analysis was performed assuming that the GTU works at 40 % part-load mode from 20 % to 50 % of the time in a year. Thus, if the fuel price is equal to \$0.17 per kg of the fuel with LHV equal 50 kJ/kg, the savings may be from \$154,000 to \$387,000 per year.

### Conclusions

– The developed GTUdT allows simulating the behavior of real GTU including off-design and part-load modes, automatically calculating compressor, turbine and entire cooling system performance, and their matching.

– The validation of proposed GTUdT with the test data for the case of different ambient temperature values was done. The validation showed good agreement of the GTUdT performance data with the real test data.

– The assessment of the possibility of cooling mass flow rate control and its influence on turbine performance was performed. The efficiency increment at 40 % of power is about 3.5 % in relative values, at the 70 %, it is about 1 %. It should be noticed that cooling air MFR was controlled for first nozzle only. It can be assumed that the cooling air MFR controlling at another flow path elements allows getting even higher efficiency increments.



– Preliminary economics analysis showed the savings are in the range from \$154,000 to \$387,000 per year. The final value of savings depends on part load mode power level and operation time percentage per year.

#### Off-the-shelf software tools utilized in the study

AxSTREAM® turbomachinery design, analysis and optimization tool [12, 13] was integrated into VGTU for simulation of compressor and turbine.

AxSTREAM NET™ 1D hydraulic networks analysis tool [14] was integrated into GTUdT for cooling system simulation.

AxSTREAM ION™ [15] system engineering infrastructure for the design of engineering systems was utilized for the development of GTUdT, including operation flowchart design, integration of the off-the-shelf and custom software tools, and execution.

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